## Deep Gamblers: Learning to Abstain with Portfolio Theory

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### $\underline{\text{Classification and the Inadequacy of } \textit{nll} \ \text{loss}}$

Want to find:  $\theta = \arg\max_{\theta} \Pr(Y|\theta)$ In practice, minimize  $negative\ log\ loss$   $(nll\ loss)$ :  $\min_{\theta} -\log p(Y|\theta)$ 









#### Intuition: Prediction as Horse Race

Horse Race with Reservation

*m* horses

Betting strategy:  $\sum_{i=1}^M b_i \quad o \quad \sum_{i=0}^m b_i$ 

Chance of winning:  $p_i$ 

Payoff if we bet on the winning horse:  $o_i$ 

Return after winning:  $S = o_i b_i \rightarrow o_i b_i + b_0$ 

Objective: maximize doubling rate:

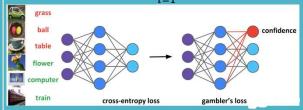
$$\max W = \max E \log(S) = \max \sum_{i=1}^{m} p_i \log(o_i b_i + b_0)$$

Classification Problem = Betting problem with Reservation with  $o=1,b_0=0$ 

Classification Problem ≤ Betting problem with Reservation

#### The proposed method: the gambler's loss

$$\max E \log(S) = \max \sum_{i=1}^{m} p_i \log(o_i b_i + b_0)$$



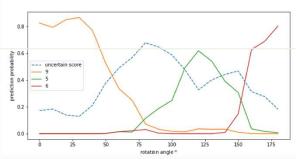
#### Toy Example: Identifying Disconfident Images...



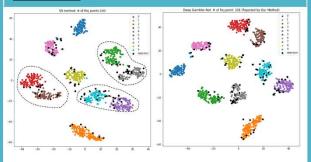
Figure 1: Top-10 rejected images in the MNIST testing set found by two methods. The number above image is the predicted uncertainty score (ours) or the entropy of the prediction (baseline). For the top-2 images, our method chooses images that are hard to recognize, while that of the baseline can be identified unambiguously by human.

#### Toy Example: Image Rotation..

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#### <u>The Learned Representation is Better</u> Separable:



(a) Normal Model

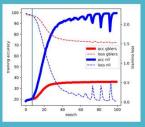
(b) Deep Gambler

#### **Surprising Benefit:**

-Training with gambler's loss reduces overfit

-Improved performance when noisy label is

present



#### SOTA Performance...

| Coverage | Ours<br>(Best Single Model) | Ours<br>(Best per coverage) | SR   | BD   | SN              |
|----------|-----------------------------|-----------------------------|------|------|-----------------|
| 1.00     | $o=2.63.24 \pm 0.09$        | -                           | 3.21 | 3.21 | 3.21            |
| 0.95     | o=2.61.36 ± 0.02            | $o=2.6$ 1.36 $\pm$ 0.02     | 1.39 | 1.40 | 1.40            |
| 0.90     | o=2.60.76 ± 0.05            | o=2.60.76 ± 0.05            | 0.89 | 0.90 | $0.82 \pm 0.01$ |
| 0.85     | o=2.60.57 ± 0.07            | $o=3.60.66 \pm 0.01$        | 0.70 | 0.71 | $0.60 \pm 0.01$ |
| 0.80     | o=2.60.51 ± 0.05            | $o=3.6$ $0.53 \pm 0.04$     | 0.61 | 0.61 | $0.53 \pm 0.01$ |

Table 3: SVHN. The number is error percentage on the covered dataset; the lower the better. We see that our method achieved competitive results across all coverages. It is the SOTA method at coverage (0.85, 1.00).

| Coverage | Ours<br>(Single Best Model) | Ours<br>(Best per Coverage) | SR   | BD   | SN              |
|----------|-----------------------------|-----------------------------|------|------|-----------------|
| 1.00     | o=2.02.93 ± 0.17            | -                           | 3.58 | 3.58 | 3.58            |
| 0.95     | o=2.01.23 ± 0.12            | $o=1.40.88 \pm 0.38$        | 1.91 | 1.92 | 1.62            |
| 0.90     | $o=2.0$ $0.59 \pm 0.13$     | $o=2.0$ $0.59 \pm 0.13$     | 1.10 | 1.10 | 0.93            |
| 0.85     | o=2.00.47 ± 0.10            | o=1.20.24 ± 0.10            | 0.82 | 0.78 | 0.56            |
| 0.80     | o=2.0 0.46 ± 0.08           | $o=2.0$ $0.46 \pm 0.08$     | 0.68 | 0.55 | $0.35 \pm 0.09$ |

Table 5: Cats vs. Dogs. The number is error percentage on the covered dataset; the lower the better. This dataset is a binary classification, and the input images have larger resolution.





